

## Learning Goals

1. To understand how to calculate a slope, given two points.
2. To determine another point on a line, given the slope and a coordinate.
3. To understand what is meant by collinear.
4. To understand how to determine if 3 or more points are collinear.

## 5.3 - Slope of a Line

Remember:  $m = \frac{y_2 - y_1}{x_2 - x_1}$  or  $m = \frac{\text{rise}}{\text{run}}$

**Example One**

Calculate the slope of the line passing through A(5, 3) and B(7, -4).

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

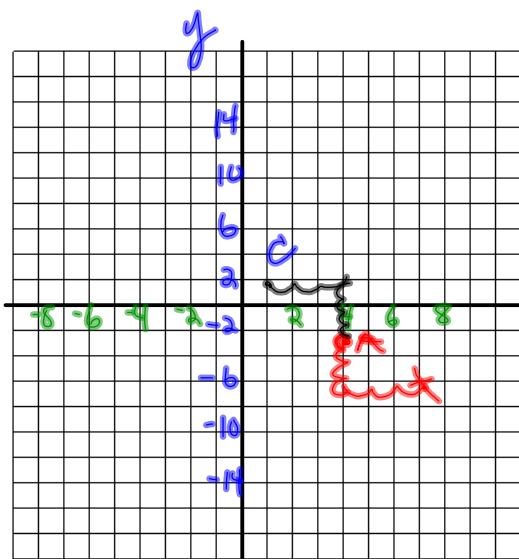
$$m = \frac{-4 - 3}{7 - 5}$$

$$m = \frac{-7}{2}$$

**Example Two**

Write the coordinates of one other point that would be on the line passing through A(4, -3) with a slope of  $\frac{-4}{3}$ .

Hint: Graph point A and then use the rise over run method to find another point.



Starting Pt:  
(4, -3)

Slope:  $\frac{-4}{3}$  (down)  
3 (right)

$\therefore$  another pt  
would be: (7, -7)

C (1, 1)

**Example Three**

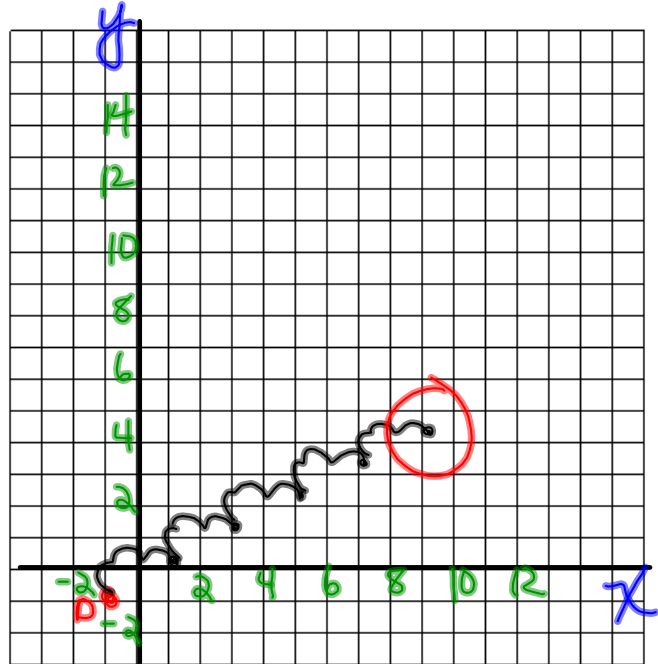
Using the graph, determine the value of "k" in point E(9, k) when  $m = \frac{1}{2}$  and the line passes through D(-1, -1).

Starting Pt

(-1, -1)

Slope:  $\frac{1}{2}$  (up)  
          2 (right)

$\therefore$  when  $x=9$ ,  
 $y=4$  or  $k=4$ .



Collinear - three or more points are collinear if they lie on the same line.

To determine if points are collinear:

1. Sketch graph of points.
2. Calculate the slope between points.
3. If all slopes are equal, then the points are collinear.

**Example Four**

Determine if the points A(-6, 12), B(3, 6) and C(12, 0) are collinear.

Slope of AB

$$A(-6, 12) \quad B(3, 6)$$

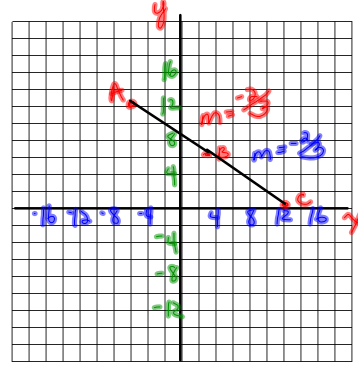
$$\begin{matrix} x_1 & y_1 & x_2 & y_2 \end{matrix}$$

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$= \frac{6 - 12}{3 - (-6)}$$

$$= \frac{-6 \div 3}{9 \div 3}$$

$$= -\frac{2}{3}$$

Slope of BC

$$B(3, 6) \quad C(12, 0)$$

$$\begin{matrix} x_1 & y_1 & x_2 & y_2 \end{matrix}$$

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$= \frac{0 - 6}{12 - 3}$$

$$= \frac{-6 \div 3}{9 \div 3}$$

$$= -\frac{2}{3}$$

$\therefore$  pt A, B & C  
are collinear  
b/c the slope  
between pts is  
equal.

**Complete:** p. 278 - 279 #1, 3ace, 4, 6ac, 7, 8, 12.