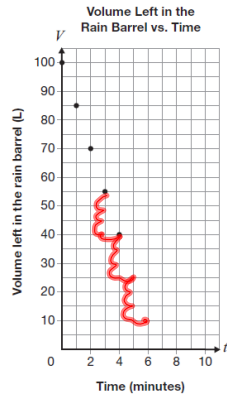


- 7 A rain barrel full of water is drained at a constant rate. Data for the first few minutes of draining is shown on the grid below.

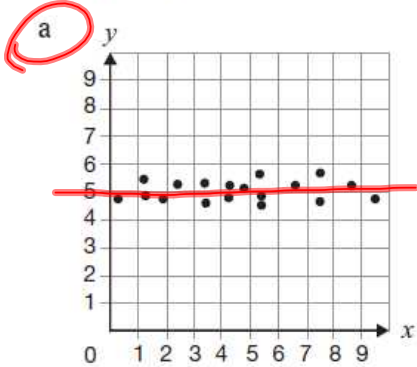


$m = -3$

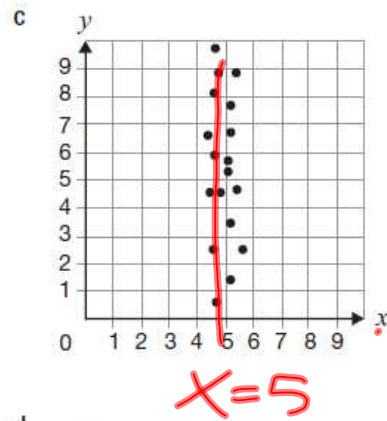
After 6 minutes, the draining is stopped. How much water is needed to refill the rain barrel?

- a 90 L
- b 75 L
- c 25 L
- d 10 L

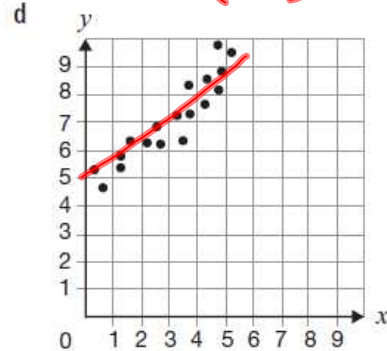
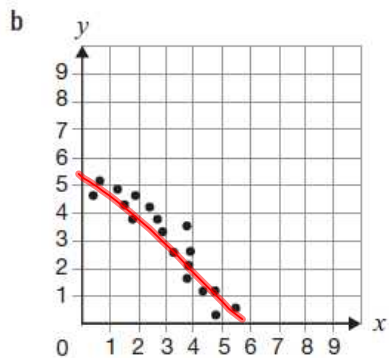
- 10 For which scatter plot could the line $y = 5$ be the line of best fit?



$y = 5$



$x = 5$



Learning Goals

1. To review the different types of triangles and quadrilaterals.
2. To review angle properties.
3. To understand that the sum of the interior angles of a triangle is 180° .
4. To understand that the sum of the interior angles of a quadrilateral is 360° .
5. To understand that the sum of the interior angles of a n-gon is $(n - 2) \times 180^\circ$.
6. To understand the properties of a regular polygon.

7.1 - Interior Angles of Polygons

Review

1. Triangles



Equilateral

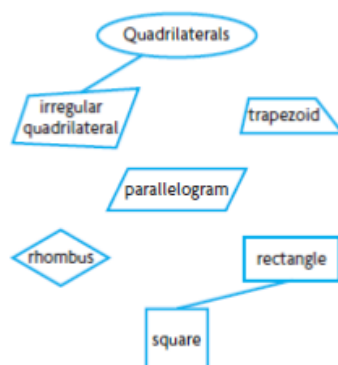


Scalene



Isosceles

2. Quadrilaterals

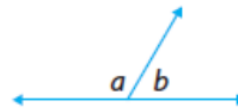


3. Angle Properties

Straight Angles

The sum of angles that form a straight angle is 180° .

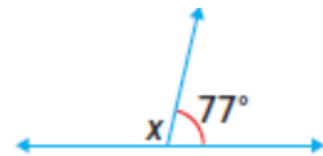
$$\angle a + \angle b = 180^\circ$$



Example One

Determine the value of the unknown angle.

$$\begin{aligned} X &= 180 - 77 \\ &= 103^\circ \end{aligned}$$

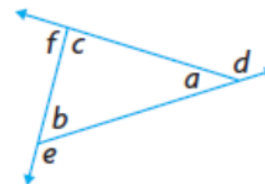


Interior and Exterior Angles of a Triangle

The sum of the interior angles in a triangle is 180° .

$$\angle a + \angle b + \angle c = 180^\circ$$

Each exterior angle equals the sum of the two interior angles opposite it.

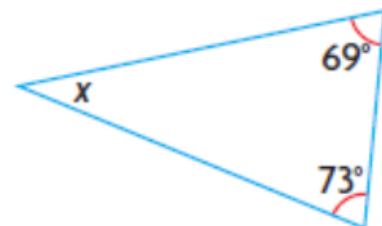


$\angle d = \angle b + \angle c$	$\angle e = \angle a + \angle c$	$\angle f = \angle a + \angle b$
----------------------------------	----------------------------------	----------------------------------

Example Two

Determine the value for the unknown angle.

$$\begin{aligned} X &= 180 - 69 - 73 \\ &= 38^\circ \end{aligned}$$



Angle Properties of Parallel Lines

When a transversal crosses 2 parallel lines:

- Corresponding angles are equal.

$$\angle a = \angle e \qquad \angle c = \angle g$$

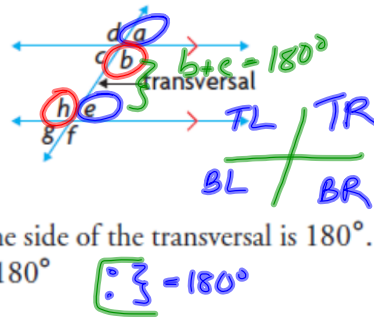
$$\angle b = \angle f \rightarrow \text{2-pattern} \qquad \angle d = \angle h$$

- Alternate angles are equal. **Z**

$$\angle b = \angle h \qquad \angle c = \angle e$$

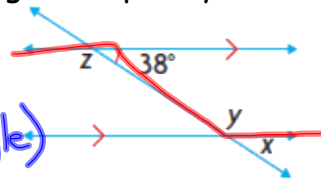
- The sum of the interior angles on the same side of the transversal is 180° .

$$\angle b + \angle e = 180^\circ \qquad \angle c + \angle h = 180^\circ \qquad \boxed{\therefore \} = 180^\circ$$



Example Three

Determine the values of the unknown angles. Explain your solution.



$$x = 38^\circ \text{ (corresponding angle)}$$

$$y = 142^\circ \text{ (interior angle)}$$

$$z = 142^\circ \text{ (alternate angle)}$$

Key Ideas

1. The sum of the interior angles of a **triangle** is 180° .
2. The sum of the interior angles of a **quadrilateral** is 360° .
3. The sum of the interior angles of a **n-gon** is $(n - 2) \times 180^\circ$.

Note: a n-sided polygon is often called an n-gon. So, a 20-sided polygon is called a 20-gon.

Example Four

What is the sum of the interior angles of a polygon with each number of sides?

a) 7 sides

$$\begin{aligned} 7\text{-gon} &= (7-2) \times 180 \\ &= 5 \times 180 \\ &= 900^\circ \end{aligned}$$

b) 10 sides

$$\begin{aligned} 10\text{-gon} &= (10-2) \times 180^\circ \\ &= 8 \times 180^\circ \\ &= 1440^\circ \end{aligned}$$

c) 24 sides

$$\begin{aligned} 24\text{-gon} &= (24-2) \times 180^\circ \\ &= 22 \times 180^\circ \\ &= 3960^\circ \end{aligned}$$

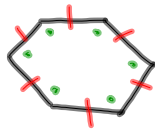
Note: A **regular polygon** has all sides equal and all angles equal.

Example Five

What is the sum of the interior angles in a regular hexagon?
What is the measure of each angle? =====

hexagon = 6 sides.

$$\begin{aligned} 6\text{-gon} &= (6-2) \times 180^\circ \\ &= 4 \times 180^\circ \\ &= 720^\circ \end{aligned}$$



Each Angle

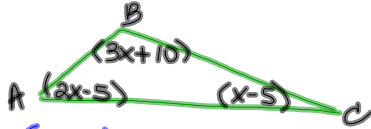
$$= 720 \div 6$$

$$= \underline{\underline{120^\circ}}$$

\therefore each angle is 120° .

Complete: p. 384 #2 - 4, 7ab
 p. 390 # 1, 2 (just calculate the sum of
 the interior angles)

p. 386 # 7a)



$$180 = (2x-5) + (3x+10) + (x-5)$$

$$180 = \underline{2x-5} + \underline{3x+10} + \underline{x-5}$$

$$\frac{180}{6} = \frac{6x}{6}, x = 30^\circ$$

$$\begin{aligned} A &= (2x-5) & B &= (3x+10) \\ &= (2 \times 30 - 5) & &= (3 \times 30 + 10) \\ &= 55^\circ & &= 100^\circ \end{aligned}$$